

1-3 Additional Practice

Piecewise-Defined Functions

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1. A phone company offers a monthly data plan for \$10 a month. The plan includes 2 megabytes of data, and charges \$0.10 per megabyte above the 2 megabytes of data.
- a. Complete a table for this scenario.

Number of megabytes	Total Cost of the Bill (\$)
0	10
1	10
2	10
3	$10 + .1(1) = 10.10$
4	$10 + .1(2) = 10.20$
5	$10 + .1(3) = 10.30$
6	$10 + .1(4) = 10.40$

(7)

- b. Write a piecewise-defined function for $M(x)$, the cost for x megabytes of data used in a month.

$$\begin{cases} M(x) = 10 & 0 \leq x \leq 2 \\ M(x) = 10 + .1(x-2) & x > 2 \end{cases}$$

(4)

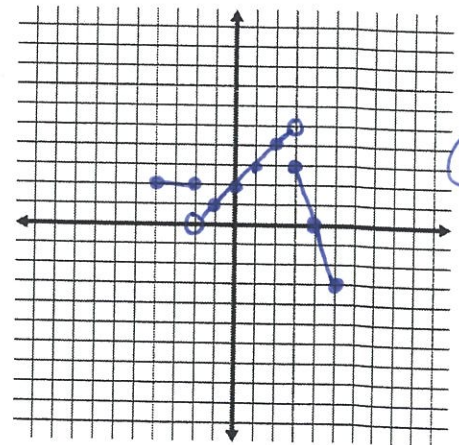
2. Graph the piecewise-defined function. State the domain and range. Identify whether the function is increasing, constant, or decreasing on each interval of the domain.

Constant $\left\{ \begin{array}{l} 2, \quad -4 \leq x \leq -2 \\ x+2, \quad -2 < x < 3 \\ -3x+12, \quad 3 \leq x \leq 5 \end{array} \right.$

Inc

Dec

$$\begin{array}{r|l} x+2 & 0 \\ -1 & 1 \\ 0 & 2 \\ 1 & 3 \\ 2 & 4 \\ 3 & 5 \end{array} \quad \begin{array}{r|l} -3x+12 & 3 \\ 4 & 0 \\ 5 & -3 \end{array}$$

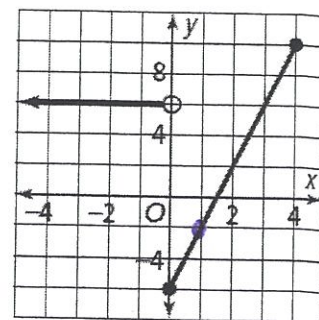


(6)

3. Write the rule that defines the piecewise-defined function in the graph.

$$\begin{cases} y = 6, & -\infty < x < 0 \\ y = 4x - 6, & 0 \leq x \leq 4 \end{cases}$$

(4)



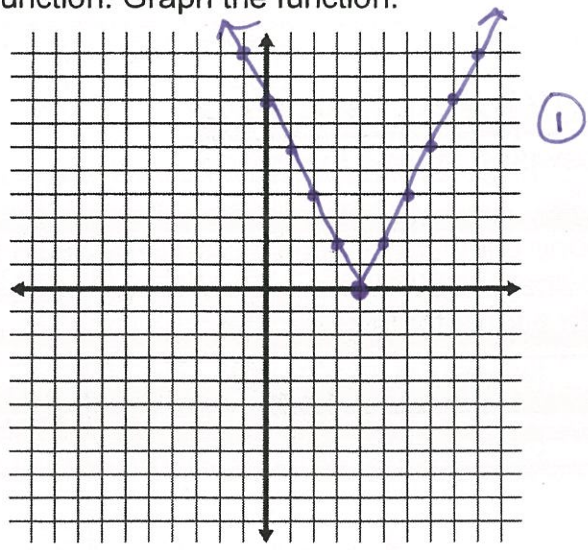
4. Write the function f as a piecewise-defined function. Graph the function.

$$f(x) = |2x - 8|$$

$$f(x) = \begin{cases} 2x - 8, & 4 \leq x < \infty \\ -2x + 8, & -\infty < x \leq 4 \end{cases}$$

$2x - 8 = 0$
 $2x = 8$
 $x = (4, 0)$

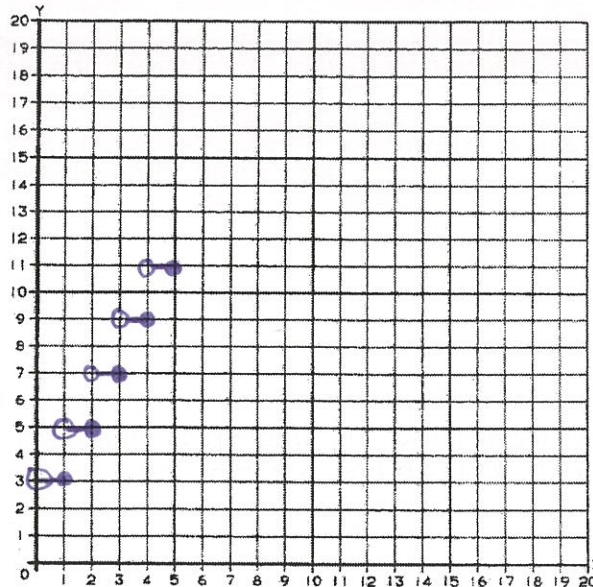
(4)



5. A shipping service uses the weight of a package to determine its postage. The charge is \$3 for the first pound and \$2 for each additional pound up to 5 pounds. What are the domain and range of the function?

$$f(x) = \begin{cases} 3, & 0 < x \leq 1 \\ 5, & 1 < x \leq 2 \\ 7, & 2 < x \leq 3 \\ 9, & 3 < x \leq 4 \\ 11, & 4 < x \leq 5 \end{cases}$$

$D: 0 < x \leq 5$
 $R: 3, 5, 7, 9, 11$



1 - open o
1 - closed o
1 - segments
(3)

What transformations of $f(x) = x^2$ are being applied to get the function g ?

6. $g(x) = 3(x + 2)^2$

(2)

skinnier
left 2

7. $g(x) = -(x - 5)^2 + 1$

(3)

reflected over x-axis
right 5
up 1

8. Derek walks to his best friend's house at a rate of 1 block per minute, then turns around and walks home. The graph shows the distance Derek walks in the given amount of time. Write an equation for the graph.

$y = -\frac{1}{2}|x - 10| + 10$ OR $\begin{cases} y = 2x, & 0 \leq x \leq 10 \\ y = -2x + 20, & 10 \leq x \leq 20 \end{cases}$

